ON THE DESIGN OF BCH CODES POLYNOMIALS FOR DIGITAL TELEVISION DVB-T2 BROADCASTING SYSTEMS

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Abstract
Digital Video Broadcasting Terrestrial–Second Generation (DVB-T2) requires a high coding rate to transmit data of high-quality video. This paper evaluates Bose-Chaudhuri-Hocquenghem (BCH) codes for the DVB-T2 to measure the gain of BCH codes. This paper evaluates the BCH codes as outer coding to be combined with other different inner encoding schemes such as Low Density Parity Check (LDPC) codes and convolutional codes to measure the best suitable inner encoding scheme. This paper also studies the performances of BCH codes for DVB-T2 specified by two different standards, i.e., (a) The European Telecommunications Standards Institute (ETSI) Technical Specification (TS) 102 831 and (b) ETSI European Standard (EN) 302 755. To obtain better error correcting capability, we propose new BCH polynomials based on the general guideline from ETSI TS 102 831 for Galois Field GF($2^{14}$). We perform computer simulations to evaluate bit-error-rate (BER) performances under additive white Gaussian noise (AWGN) channel and Indonesia DVB-T2 channel model. We revealed the superiority of BCH codes in high data rate transmission, which is required for DVB-T2, and found that BCH codes are better suited to the LDPC codes as inner encoding rather than to the convolutional codes. We also confirmed that BCH codes of DVB-T2 from ETSI TS 102 831 using the proposed BCH polynomials have better performances compared to the standard polynomial of ETSI EN 302 755. We are expecting that the obtained polynomials can be adopted by the BCH codes of Indonesia DVB-T2 system. These results are expected to support the Indonesian government in determining the parameters of the BCH codes of DVB-T2 for Indonesia.

Keywords: BCH codes; Generator polynomial; DVB-T2; FEC Encoding; Broadcasting System.

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1. Introduction
Indonesia has been using analog television transmitters for more than 60 years which has worked well. However, this technology has now turned into a digital television transmitter. In 2007, Indonesia used the Digital video broadcasting terrestrial (DVB-T) digital television standard \cite{1}. The rapid development of digital television in the world has made Indonesia chooses to change from DVB-T to Digital video broadcasting terrestrial–second generation (DVB-T2) owned by the European Telecommunications Standards Institute (ETSI) since 2012 \cite{2}. The DVB-T2 standard was developed to have 60% higher data rate. To realize it, DVB-T2 can use up to 256 quadrature amplitude modulation (QAM) with 32K fast fourier transform (FFT) size, rotated constellation, Cyclic Prefix–Orthogonal Frequen-
cies Division Multiplexing (CP-OFDM), and new system of Forward Error Correction (FEC). Based on [3], DVB-T2 in Indonesia uses tuning frequency of 478–694 MHz, channel bandwidth of 8 MHz, modulation of QPSK–256 QAM, FFT size of 1K–32K, and TV stations of 22–48 units.

Research in [4] proposes FEC encoding using Low-Density Parity Check (LDPC) codes with Bit-Interleaved Coded Modulation (BICM) schemes. However, this paper uses FEC encoding with a combination of 2 types of coding, i.e., outer coding and inner coding [5]. This paper focuses on the outer coding of FEC encoding DVB-T2. High coding rate is used for outer coding of DVB-T2 to transmit data for high-quality video without jitter [6]. Standard of DVB-T2 uses Base, Chaudhuri, Hocquenghem (BCH) codes as outer coding of FEC encoding [6].

ETSI publishes several types of standards for DVB-T2 including the European Standard (EN) and Technical Specification (TS). Between the two types of standards, we found that the specification of BCH codes from TS is completely different from EN. In TS 102 831 [7], BCH polynomials are generated based on GF(214) with error correction capability t = 12 for short FECFRAME. However, in EN 302 755 [6], BCH polynomials have been provided to be a generator polynomial of BCH codes DVB-T2. In this paper, we study the structure of BCH codes of DVB-T2 for Indonesia including the coding gain of BCH codes as the outer coding of DVB-T2. We directly study BCH codes polynomials on the TS and EN standards of DVB-T2 technology. We also evaluate the suitable inner coding DVB-T2 pairing with the BCH codes.

To have a better performance of digital Television in Indonesia, we propose BCH codes polynomials based on the general guideline on TS. Our contributions are summarized as follows:

1. BCH polynomials for GF(214) are proposed to provide better performance with higher coding gain.
2. BER performances of DVB-T2 outer coding are investigated.
3. BER performances of DVB-T2 total coding constructed from inner and outer coding schemes are evaluated.
4. BER performances of DVB-T2 BCH codes under Indonesia digital TV channel model are evaluated.

The rest of this paper is organized as follows. Section 2 discusses the system model of DVB-T2. In Section 3, we propose BCH polynomials for BCH codes DVB-T2. Performances are evaluated and analyzed in Section 4. Finally, the conclusions are provided in Section 5 with some concluding remarks.

2. System Model of DVB-T2

Fig. 1 shows the system model of communication systems in DVB-T2. BCH codes are used as outer coding of FEC encoding. We consider DVB-T2 modulation using Quadrature Phase Shift Keying (QPSK) and multipath fading channel model based on Bandung DVB-T2 channel model used in [8]. We also consider Orthogonal Frequency Division Multiplexing (OFDM) based on the DVB-T2 standard.

In Fig. 1, the bit stream b is generated randomly for the number of bits of information k_BCH. We encode bits b by multiplying x_{BCH} to generate the message polynomial m(x). In the construction of BCH codes, g(x) block form a polynomial generator. The quotient of m(x) divided by the polynomial generator g(x) is used to be parity check bits. Adding the polynomial message m(x) to parity check bits produces the codeword C_{BCH} = (C_1, C_2, \ldots, C_N), where N is blocklength of DVB-T2 BCH codes. Then, C_{BCH} encoded with inner encoder to obtain codeword from FEC encoding.

Codeword of FEC encoding C_{inner} is mapped and modulated into modulator M to produce x_m symbol. The Inverse Fast Fourier Transform (IFFT) FH with 4096 FFT-size is used to transform x_m to symbol x. The block "CP" adds cyclic prefix (CP) in x with length equal to the number of paths. OFDM symbols x_{cp} are transmitted through multipath channel H. At the receiver, a noise n is added and the received signal y_{cp} can be expressed as

\[ y_{cp} = h \cdot x_{cp} + n, \]

where the received signal y_{cp} is corrupted by noise n, which is modeled by Gaussian distribution. CP in y_{cp} is removed in CP Removal block to generate y. The Fast Fourier Transform (FFT) is conducted in F block to generate y_e; the y_e is then equalized in EQ block using mean minimizes squared error (MMSE) [9] to become y_m; the y_m is then demodulated by M^{-1} block into expected codeword \hat{C}_{inner} from FEC decoding. Inner decoder will obtained \hat{C}_{BCH} to be decoded by BCH decoder. In the BCH decoder block, \hat{C}_{BCH} can be used to calculate the syndrome. Furthermore, the value of the syndrome is used to determine the location of the error polynomial c(y) and can also find the error position a'. Delay is used to
compensate for the delay in utilization. From BCH decoder obtained bit source \( b \).

In this paper, we compare the \( b \) in the receiver with \( b \) to obtain BER performances of DVB-T2 system. The theoretical BER in Rayleigh fading channels with QPSK modulation is expressed as [10]

\[
P_{b_{QPSK-fading}} = \frac{1}{2} \left[ 1 - \frac{1}{\sqrt{1 + \frac{E_b}{N_0}}} \right],
\]

(2)

where \( \frac{E_b}{N_0} \) is the energy bit per noise spectral density, of which the signal-to-noise power ratio (SNR) for QPSK is defined as

\[
\gamma = 2 \cdot R \cdot \frac{E_b}{N_0}
\]

(3)

with \( R \) being the channel coding rate.

### 3. The Proposed BCH Polynomials for BCH Codes DVB-T2

The proposed BCH polynomials is shown in Table 1, where the polynomials are generated from \( GF(2^{14}) \) [7]. Elements for \( GF(2^{14}) \) are expressed with \( \alpha \) as the polynomial

\[
\alpha^i \Rightarrow x^i \mod \varphi(x)|_{x=\alpha},
\]

(4)

where \( \varphi(x) \) is primitive polynomial. We use primitive polynomial of \( GF(2^{14}) \) is [11]

\[
\varphi(x) = 1 + x + x^6 + x^{10} + x^{14}.
\]

(5)

Let \( O(x) \) be an irreducible polynomial over \( GF(2^m) \). If \( O(x) \) has \( \beta \) as its root, where \( \beta \) is an element in \( GF(2^{14}) \), then \( O(x) \) is the minimum polynomial of \( \beta \). The minimum polynomial of \( \beta \) can be obtained as

\[
O(x) = \prod_{i=0}^{L-1} (x - \beta^i),
\]

(6)

where \( L \) is the smallest integer such that \( \beta^{2^L} = \beta \). The generator polynomial of a BCH code DVB-T2 is the least common multiple (LCM) of the minimum polynomials of \( O(x) \) [12],

\[
g(X) = LCM(O_1(x), O_2(x), \ldots, O_L(x)),
\]

(7)

where \( O_i(x) \) represents the BCH polynomials of each \( g_i(x) \) with \( t = 1, 2, \ldots, 12 \).

BCH codes of DVB-T2 encodes information bits into a codeword [6] with the following steps:

1. Multiply the information bit \( M \)

\[
M = M_{K_{bch}}x^{K_{bch}-1} + M_{K_{bch}-2}x^{K_{bch}-2} + \cdots + M_1x + M_0,
\]

(8)
by the generator polynomial \( g(x) = x^{N_{bch} - K_{bch}} \).

2. Divide \( M \) by \( g(x) \) to produce the remainder of the division \( d(x) \) as
\[
d(x) = d_{N_{bch} - K_{bch} - 1} x^{N_{bch} - K_{bch} - 1} + \cdots + d_1 x + d_0. \tag{9}
\]
3. Construct codeword \( c(x) \) to be output for the \( \text{BCH} \) encoder as
\[
c(x) = x^{N_{bch} - K_{bch}} m(x) + d(x). \tag{10}
\]

4. Performance Evaluations

In this section, we verify the BER performances of DVB-T2 BCH codes, DVB-T2 FEC encoding, and \( \text{BCH} \) polynomials in AWGN channel. We also verify BER performances of DVB-T2 BCH codes using the proposed \( \text{BCH} \) polynomials in Bandung DVB-T2 channel model. We analyze the BER performances using computer-based simulation. BER performance is measured by taking the ratio between the number of bit error at the receiver side and the number of bits have been transmitted and is defined as
\[
P_b = \frac{u}{(k \times f)} \tag{11}
\]
where \( u \) is total error bits, \( k \) is number of bits transmitted, and \( f \) is the frame of each trial.

4.1 BER Performances of DVB-T2 BCH codes

This section evaluates the BER performances of DVB-T2 outer coding using \( \text{BCH} \) codes compared with punctured convolutional codes. Fig. 2 shows that the red box is a deleted bits derived from coding rate \( R = 1/2 \) convolutional codes [13, 14] with constraint length \( K = 2 \) and generator \( G = ([1], [10]) \). Fig. 3 shows the BER performances of DVB-T2 outer coding in AWGN channel with length of information \( k = 7032 \) and blocklength \( N = 7200 \). The horizontal axis is the SNR \( \gamma \), while the vertical axis is the BER \( P_b \). The BER performances of \( 10^{-4} \) is obtained by LDPC codes at \( \gamma = 8.5 \) dB, while convolutional codes have a gap of 3.9 dB from the Shannon limit. LDPC codes produce a turbo cliff at \( \gamma = 0.5 \) dB because of the matching between the extrinsic information trans ver (EXIT) curves of the variable node and check node [15]. The \( \text{BCH} \) codes and LDPC codes as outer and inner coding, respectively, provide the best performance because \( \text{BCH} \) codes can achieve the highest coding gain leading to a performance of both having a gap to Shannon limit below 3 dB.

4.2 BER Performances of DVB-T2 FEC encoding

We have simulated the BER performance of FEC encoding with \( \text{BCH} \) codes as outer coding followed by the different inner coding schemes such as LDPC codes and convolutional codes in AWGN channel. Fig. 4 shows the BER performances of DVB-T2 FEC encoding with coding rate of outer coding \( R_{outer} = 7032/7200 \), coding rate of inner coding \( R_{inner} = 1/2 \). The horizontal axis is the BER \( P_b \). The BER performances of \( 10^{-4} \) is achieved by LDPC codes at \( 1.65 \) dB, by \( \text{BCH} \) codes at \( 8.5 \) dB, by convolutional codes at \( 4.4 \) dB, and by \( \text{BCH} \) codes at \( 4 \) dB.

These results indicate that \( \text{BCH} \) codes can improve the performance of LDPC codes by achieving a coding gain of 0.85 dB, while convolutional codes only provide a coding gain of 0.4 dB. \( \text{BCH} \) codes outperform LDPC codes at BER of \( 10^{-4} \) have a gap from the Shannon limit of 1.8 dB, where \( \text{BCH} \) + convolutional codes have a gap of 3.9 dB from the Shannon limit. LDPC codes produce a turbo cliff at \( \gamma = 0.5 \) dB because of the matching between the extrinsic information trans ver (EXIT) curves of the variable node and check node [15]. The \( \text{BCH} \) codes and LDPC codes as outer and inner coding, respectively, provide the best performance because \( \text{BCH} \) codes can achieve the highest coding gain leading to a performance of both having a gap to Shannon limit below 3 dB.

4.3 BER Performances of BCH polynomials

We evaluate the BER performances of \( \text{BCH} \) codes using the proposed \( \text{BCH} \) polynomials from ETSI TS 102 831 compared to BCH polynomials from EN 302 755 at Table 2. Fig. 5 shows that the BER performances of \( 10^{-4} \) is achieved by \( \text{BCH} \) polynomials with ETSI EN 302 755 at \( \gamma = 11.35 \) dB and by ETSI TS 102 831 at \( \gamma = 9.7 \) dB. The BER performances of \( \text{BCH} \) codes using the proposed \( \text{BCH} \) polynomials have good performances with an improvement of 1.75 dB better than the \( \text{BCH} \) polynomials of ETSI EN 302 755.

We also evaluate the BER performances of DVB-T2 BCH codes using the proposed \( \text{BCH} \) polynomials at Table 2.

### Table 2: BCH Polynomials of ETSI EN 302 755

| \( g_1(x) \) | \( 1 + x + z^2 + z^3 + z^{14} \) |
| \( g_2(x) \) | \( 1 + x^2 + x^3 + x^{11} + z^{14} \) |
| \( g_3(x) \) | \( 1 + z^2 + z^3 + z^4 + z^{10} + z^{14} \) |
| \( g_4(x) \) | \( 1 + z^2 + z^3 + z^4 + z^6 + z^{10} + z^{14} \) |
| \( g_5(x) \) | \( 1 + z^2 + z^3 + z^4 + z^{10} + z^{14} \) |
| \( g_6(x) \) | \( 1 + z^2 + z^3 + z^4 + z^{10} + z^{14} \) |
| \( g_7(x) \) | \( 1 + z^2 + z^3 + z^4 + z^{10} + z^{14} \) |
| \( g_8(x) \) | \( 1 + z^2 + z^3 + z^4 + z^{10} + z^{14} \) |
| \( g_9(x) \) | \( 1 + z^2 + z^3 + z^4 + z^{10} + z^{14} \) |
| \( g_{10}(x) \) | \( 1 + x + z^2 + z^3 + z^4 + z^6 + z^7 + z^{10} + z^{13} + z^{14} \) |
| \( g_{11}(x) \) | \( 1 + x + z^2 + z^3 + z^4 + z^6 + z^7 + z^{10} + z^{13} + z^{14} \) |
| \( g_{12}(x) \) | \( 1 + z^2 + z^3 + z^4 + z^6 + z^7 + z^{10} + z^{13} + z^{14} \) |

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Fig. 2. Block structure of convolutional codes with rate $R = 7032/14064$ to be punctured to obtain new rate $R = 7032/7200$.

Fig. 3. BER performances of BCH codes compared to that of the convolutional codes with $N_{outer} = 7200$ in AWGN channel.

Fig. 4. BER performance of 2 inner coding schemes, i.e., BCH+LDPC codes and BCH+convolutional codes with $N_{inner} = 16200$ in AWGN channel.

polynomials, of which the result is expected to be used as a reference for DVB-T2 system implementation, especially for outer coding of DVB-T2 in Indonesia.

Fig. 5. BER performances of BCH codes with the proposed polynomials with $N_{outer} = 7200$ in AWGN channel.

Fig. 6 shows the BER performances of OFDM with CP length 8 and FFT size of 4096 under Bandung DVB-T2 channel model [8]. The horizontal axis is the average SNR $\gamma$, while the vertical axis is the average BER. The theoretical BER of uncoded Rayleigh fading is shown as the baseline comparison. We found that the BER performances of uncoded DVB-T2 has better performance than the uncoded theoretical Rayleigh fading with QPSK modulation caused by the multipath fading gain captured by the OFDM system. The BER performances of $10^{-3}$ is achieved by DVB-T2 BCH codes with $N_{outer} = 7200$ at $\gamma = 25.2$ dB with an improvement, which is expected to be significant at higher SNR due to the high channel coding rate.
5. Conclusion

We have studied several aspects of BCH codes, e.g., polynomials and coding gain, of DVB-T2 systems. We performed computer simulations to evaluate BCH codes and found that the BCH codes have better performance than convolutional codes as outer coding scheme of DVB-T2 with a coding gain of 1.75 dB. We also evaluated the contribution of BCH codes as outer coding and paired with inner coding schemes of LDPC codes and convolutional codes constructing BCH+LDPC codes and BCH+convolutional codes, respectively. BCH+LDPC codes have better performances than BCH+convolutional codes because LDPC codes are capable of producing turbo cliffs performances resulted from the matching between the extrinsic information transfer curve of variable node and check node.

This paper has also proposed new BCH polynomials generated from GF(2^{14}) for DVB-T2 BCH codes, where we have confirmed that The proposed BCH polynomials have better performances compared to polynomials of ETSI EN 302 755. The proposed BCH polynomials are different compared to polynomial of ETSI EN 302 755 in every degree. This paper also evaluated the performances of DVB-T2 BCH codes under the Indonesian digital TV channel model to estimate the performances in Indonesia. The results of this paper are expected to provide contributions to the development and implementation of Indonesia digital TV.

References


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